

# STATENS GEOTEKNISKA INSTITUT

SWEDISH GEOTECHNICAL INSTITUTE



# SÄRTRYCK OCH PRELIMINÄRA RAPPORTER

REPRINTS AND PRELIMINARY REPORTS

Supplement to the "Proceedings" and "Meddelanden" of the Institute

# Some Experiments on Hollow Cylinder Clay Specimens

A. K. Jamal

STOCKHOLM 1972



Manager and a second second

A NOT AND ANY



# STATENS GEOTEKNISKA INSTITUT

SWEDISH GEOTECHNICAL INSTITUTE

# No. **47**

# SÄRTRYCK OCH PRELIMINÄRA RAPPORTER

## REPRINTS AND PRELIMINARY REPORTS

Supplement to the ''Proceedings'' and ''Meddelanden'' of the Institute

# Some Experiments on Hollow Cylinder Clay Specimens

A. K. Jamal

•

.

.

.

.

#### PREFACE

This report describes some experiments with hollow cylindrical specimens which the Author had performed at the Swedish Geotechnical Institute in 1966-67. At that time he had submitted his Ph.D. Thesis at Cornell University, USA. Earlier during the period 1961-64, the Author had been associated with the hollow cylinder test programme at Cornell University, Department of Soil Engineering which was conducted under the general direction of Dr. B.B.Broms for testing undrained soil cylinders. Subsequent to 1964, the Author's primary research effort was directed at understanding of the drained hollow cylinder test. The experiments reported herein were continuation of the Author's research project.

This research work was partly supported through a grant from the Swedish National Council for Building Research (BFR Grant C 202:2Db).

Stockholm, December 1972 SWEDISH GEOTECHNICAL INSTITUTE

.

~

## CONTENTS

### PREFACE

.

•

.

٠

٠

SY	NOPSIS	1
1	INTRODUCTION	3
2	TEST APPARATUS AND PROCEDURES	4
	Hollow Cylinder Specimens	4
	Hollow Cylinder Specimen Preparation	7
	Solid Cylinder Specimens	9
	Consolidation under Hydrostatic Pressure	9
	Undrained Axial Compression	10
3	EXPERIMENTAL RESULTS	10
	Consolidation under All-round Hydrostatic Pressure	10
	Undrained Axial Compression Tests	15
4	SUMMARY	18
AC	KNOWLEDGEMENTS	18
AP	PENDIX. Formulae for Strain and Stress Computations in Hollow Cylinder Specimen	19

\_

# SOME EXPERIMENTS ON HOLLOW CYLINDER CLAY SPECIMENS By A.K. Jamal, Swedish Geotechnical Institute

#### SYNOPSIS

A hollow cylinder apparatus for moulded soil specimens with 60 mm outside and 35 mm inside diameter is described in this report. Experimental results of hollow cylindrical specimens of undisturbed clay are presented. The clay cylinders with lubricated ends were consolidated hydrostatically and loaded in axial compression under undrained condition with pore-water pressure measurement. For reference, solid cylinders of 35 mm and 60 mm diameter of the same clay were also tested. Hollow cylinder tests were performed with either

- 1) equal outside and inside chamber pressures, or
- 2) constant volume of the inside chamber.

KEY WORDS: Hollow cylinder testing, shear strength, undisturbed clay cylinders, consolidation under hydrostatic pressure, undrained axial compression.



#### 1. INTRODUCTION

Hollow cylindrical specimens are used to study the strength and deformation properties of soil and other compressible materials in a generalized stress field. In the hollow cylinder test, the magnitude, orientation and application of the three principal stresses can be varied independently in any prescribed manner by varying the inside and the outside chamber pressures and the axially applied load. The direction of the principal stress axes can be changed through the application of a torque to the two end surfaces of the cylindrical specimen. The hollow cylinder test in this respect is superior to the standard triaxial test for which solid cylinder specimens are used. However the hollow cylinder behaviour under stress application is influenced by many factors, as for example, the test cylinder geometry and the test boundary conditions. Even for simpler stress systems the hollow cylinder behaviour is necessary for rational interpretation of material property determinations using hollow cylindrical specimens.

This investigation was undertaken to study the hollow cylinder behaviour for particular stress applications and to gain a better understanding of the hollow cylinder test. Undisturbed clay samples were used. Both solid and hollow cylindrical specimens with lubricated end contacts were tested. The test cylinders were consolidated hydrostatically and loaded axially in compression under undrained state. The pore-water pressure changes in the clay during axial compression were measured.

Some 38 tests on cylinders with three different configurations were performed. Dimensions of the test specimens are given in Table 1. Only representative test results of each cylinder configuration will be presented in this report.

Table 1.	Test	cylinder	dimensions
----------	------	----------	------------

Specimen configuration	Outside diameter mm	Inside diameter mm	Height mm	Number of tests
Solid cylinder	35		60	9
Solid cylinder	60	-	60	8
Hollow cylinder	60	35	60	21

Clay samples for this study were obtained from the test site at Skå Edeby of the Swedish Geotechnical Institute. Clay cores of 60 mm diameter were extracted from a depth of between 4 m and 6.7 m in three closely spaced boreholes using a piston sampler which was provided with thin liner tubes.<sup>1)</sup>

This report is confined to a presentation of the factual information only.

## 2 TEST APPARATUS AND PROCEDURES

Hollow Cylinder Specimens. The hollow cylinder apparatus used in this study is shown in Figs. 1 and 2. A standard Geonor triaxial cell was used which was modified to test hollow samples with 60 mm outside diameter and 35 mm inside diameter, and a maximum height of about 100 mm.

The test specimen is jacketed between an outer and an inner rubber membrane and supported at top and bottom by rigid ring shaped platens. The contact of the specimen with end platens is made over a sandwich of lubricated thin rubber

<sup>1)</sup> The in-situ properties of the Skå Edeby clay have been described in several of the Institute's publications, for example in HANSBO, S., 1960. Consolidation of Clay, with Special Reference to Influence of Vertical Sand Drains. Swed. Geot. Inst. Proc. No. 18.



Fig. 1 Hollow cylinder apparatus for clay cylinders

.

4

-



Fig. 2 Component parts of the hollow cylinder apparatus

ţ





## Fig. 3

(a) above. Brass sleeve containing clay core is mounted on stand;1 cm dia. hand auger and curved blade

(b) above right. Hollow cylinder specimen contained in brass sleeve is assembled on test platen

(c) below right. Brass sleeve removed and filter paper strips wrapped around the cylinder surface



sheets placed over smooth teflon discs which in turn rested upon porous metal rings as shown in Fig. 1. By this manner contact friction between the specimen and the test platens was minimized. Thin strips of filter paper with about 10 mm width were wrapped around the outer circumference of the clay cylinder, see Fig. 3c. The filter paper strips extended to porous metal rings at top and bottom to provide drainage during consolidation of the clay cylinder.

A load hanger assembly was designed, as shown in Fig. 1, to measure axial deformations of the test cylinders during the consolidation phase of each test. A dial gauge was mounted on the plunger. Counter-weights equal to the uplift force exerted upon the plunger by the hydrostatic pressure were added to the loading pan so that the plunger remained in contact with the test specimen cap during consolidation.

<u>Hollow Cylinder Specimen Preparation</u>. The hollow specimens were prepared by first placing the 60 mm diameter clay core, contained in a brass sleeve, between two plates on a vertical stand as shown in Fig. 3a. Each plate had a hole of 35 mm diameter at the centre. A small pilot hole of about 10 mm diameter was made through the centre of clay core with a small auger. This hole was then enlarged to 35 mm diameter by gradually removing the clay in thin circumferential slices using a sharp blade.

The tubular clay sample contained in brass sleeve was thereafter placed on the lubricated pedestal of the base plate, as shown in Fig. 3b. The upper pedestal was assembled making sure that the inner rubber membrane was in contact with the inside face of the tubular core. The brass sleeve was then removed and filter paper strips were wrapped around the outer surface, Fig. 3c. The outside rubber membrane was thereafter placed around the sample. The test specimen was sealed then by O-rings stretched over the top and bottom pedestals.

Freshly boiled water was circulated slowly from the bottom to the top of the test specimen to displace air bubbles which might become entrapped in the test cylinder during setting-up. The sealed test cylinder was next subjected to a negative pressure by lowering the drainage burette about 10 mm, to remove the excess water which had accumulated during saturation of the test cylinder.





.

.

The inner chamber of the tubular cylinder was then filled with water. The top sealing cap was attached while the water was overflowing from the inner chamber.

<u>Solid Cylinder Specimens</u>. Solid cylinder specimens with 35 mm and 60 mm diameter were tested in standard Geonor triaxial apparatus. The 35 mm test cylinders were trimmed from the 60 mm core samples.

The friction at top and bottom of the specimen was minimized by the use of thin rubber sheets which were smeared with silicone grease and a smooth teflon disc inserted between the test cylinder and the porous stones, in the same manner as described for the hollow cylindrical specimen. Filter paper strips were wrapped around the specimen circumference to facilitate pore water drainage to the upper and lower porous plates.

<u>Consolidation under Hydrostatic Pressure</u>. All specimens were consolidated for about 22 hours at an all-round pressure of  $2 \text{ kg/cm}^2$  (200 kN/m<sup>2</sup>), which was applied in one increment. Arrangement of the test apparatus during consolidation and during axial compression phases of the test is shown schematically in Fig. 4.

For all specimens, axial deformations  $\Delta h$  and volume changes ( $\Delta V$ )<sub>s</sub> were measured during the consolidation. Recordings of these deformation parameters were made at regular intervals of time during the initial phase of consolidation, over a period of about 8 hours.

Some of the hollow clay cylinders were consolidated at inside chamber pressure  $\sigma_{ri}$  which was equal to the outside chamber pressure  $\sigma_{ro}$ . For this case with equal boundary radial stresses  $\sigma_{ro} = \sigma_{ri}$  the volume changes ( $\Delta V$ ); of the inner chamber were measured by a gauge connected in series with the constant cell pressure system as shown in Fig. 4.

The volume of the inner chamber was held constant for the remainder of the hollow cylinder tests. The resulting pressure changes  $\Delta G_{ri}$  in the inner chamber were measured by a null indicator and a differential mercury manometer (see Fig. 4) which registered the pressure difference between the outer and the inner chamber of the hollow cylinder.

<u>Undrained Axial Compression</u>. At the completion of consolidation, the test cylinders were subjected to axial compression at a constant strain rate of approximately 0.03 percent per min. The pore-water pressures generated in the test cylinders were recorded. The compression tests were terminated, generally, when the axial load measured by proving ring reached a terminal value.

Some of the hollow cylinders were tested in axial compression with equal outside and inside chamber pressures. The corresponding volume changes ( $\Delta V$ ); for the inner chamber were recorded. Generally the hollow cylinders which had been consolidated at equal chamber pressures  $\sigma_{ro} = \sigma_{ri}$  were also tested in axial compression at equal chamber pressures  $\sigma_{ro} = \sigma_{ri}$ .

The hollow cylinders which had been consolidated at constant volume of the inner chamber were tested in axial compression at constant volume of the inner chamber. The inner chamber was sealed during these tests. The corresponding pressure changes,  $\Delta \sigma_{ri}$ , in the inner chamber were recorded as during the consolidation phase of test.

#### 3 EXPERIMENTAL RESULTS

Experimental results from four representative tests of each specimen configuration are presented herein. The stress and strain parameters for each test were computed as per the formulae given in the Appendix. For convenience the test results for consolidation and axial compression phases of each test are treated separately.

Consolidation under All-round Hydrostatic Pressure. The volumetric strain  $(\Delta V/V)_s$ , axial strain  $\mathcal{E}_z$ , as well as the boundary strains  $\mathcal{E}_{\Theta \circ} = \mathcal{E}_{r\circ}$  for the solid cylinder specimens during consolidation are shown in Figs. 5 and 6. The consolidation behaviour of the solid clay cylinders with 35 mm and 60 mm diameter show similar characteristics. The boundary strains  $\mathcal{E}_{\Theta \circ} = \mathcal{E}_{r\circ}$  at the completion of consolidation were approximately equal to the axial strain  $\mathcal{E}_z$ .



Fig. 5 Consolidation test parameters. Solid cylinder specimen dia. 35 mm

.



Fig. 6 Consolidation test parameters. Solid cylinder specimen dia. 60 mm



Fig. 7a Consolidation test parameters. Hollow cylinder specimen with drained inner chamber and  $\sigma_{ro} = \sigma_{ri}$ 



Fig. 7b Principal strains during consolidation. Hollow cylinder specimen with drained inner chamber and  $\sigma_{ro} = \sigma_{ri}$ 



Fig. 8a Consolidation test parameters. Hollow cylinder specimen with undrained inner chamber



Fig. 8b Principal strains during consolidation. Hollow cylinder specimen with undrained inner chamber

Test results of hollow cylinder specimen consolidated under equal outside and inside chamber pressures,  $\sigma_{ro} = \sigma_{ri}$ , are shown in Figs. 7a and 7b. It is seen that the measured volumetric strain  $(\Delta V/V)_i$  for the inner chamber is lower than the clay cylinder strain  $(\Delta V/V)_s$  for the entire consolidation period. The volumetric strains  $(\Delta V/V)_i$  and  $(\Delta V/V)_s$  have been converted into the average strains<sup>2)</sup>  $\varepsilon_{\theta}$  and  $\varepsilon_r$  and the latter are plotted in Fig. 7b. It is noted that the radial strain  $\varepsilon_r$  is about two to three times the circumferential strain  $\varepsilon_{\theta}$ . This constitutes a significant experimental finding<sup>3)</sup>. This behaviour was consistently noted for all hollow samples which were consolidated under equal outside and inside chamber pressure condition of  $\sigma_{re} = \sigma_{ri}$ .

Figs. 8a and 8b show the consolidation results of hollow cylinder specimen when the inner chamber volume was kept constant. The important finding here is that the inner chamber pressure  $\sigma_{ri}$  which is equal to the radial stress at the inside face of specimen, increased during the consolidation relative to the constant outer chamber pressure  $\sigma_{ro}$ . An increase in inner radial stress  $\Delta\sigma_{ri}$ , of between 10 to 15 percent of the constant maintained  $\sigma_{ro}$  was consistently noted for all hollow clay cylinders which were consolidated under this boundary condition. The computed radial strain  $\varepsilon_r$ , for this test case is about seven times the corresponding circumferential strain  $\varepsilon_{\theta}$  as shown in Fig. 8b.

Apart from the noted differences in the circumferential and radial strains  $\varepsilon_{\Theta}$ and  $\varepsilon_{r}$ , and the increase in inner radial stress  $\Delta \sigma_{ri}$ , a consistent pattern of variation in other of the test parameters e.g. the volumetric strain ( $\Delta V/V$ )<sub>s</sub>

<sup>2)</sup>  $\varepsilon_{\theta}$  and  $\varepsilon_{r}$  as well as  $\varepsilon_{z}$  and ( $\Delta V/V$ ) have been expressed as absolute . strains in this study. The use of natural strains instead of absolute strains as deformation parameters is of little significance for the purpose of this study.

<sup>3)</sup> Mathematical theory of inequality of the strains  $\varepsilon_{\theta}$ ,  $\varepsilon_{r}$  with volumetric change in right cylinder specimen is given in:

JAMAL, A.K., 1966. The Distribution of Radial Stress in the Triaxial Strength Test of a Cohesionless, Granular Soil. Thesis submitted to Cornell University, USA, in September 1966, in partial fulfillment of the requirements for the degree of Doctor of Philosophy.

or the axial strain  $E_z$ , could not be discerned in the present series of hollow cylinder experiments with constant pressure or constant volume condition of the inner chamber. It was also not possible to relate the hollow specimen consolidation parameters to the corresponding solid specimen parameters. A clearer picture of the consolidation test parameters is, in this respect, difficult to form because of the previous stress history of the in-situ extracted samples as well as the random variations in their natural properties.

<u>Undrained Axial Compression Tests</u>. Results of the axial compression tests on solid cylinder specimens are presented in Figs. 9 and 10. These are notable chiefly for the differences in pore-water pressure variations in the test specimens with 35 mm and 60 mm diameter, as reflected by the effective radial stress  $\sigma'_{ro}$ . The maximum deviator stress  $\sigma'_{z ext}$ , was approximately equal for the two test cylinders. Also the stress ratio ( $\sigma'_{z}/\sigma'_{ro}$ ) variations show similar characteristics.

It can be seen from Figs. 11 and 12 for the hollow cylinder compression tests, that the deviator stress  $G'_{z ext}$  is somewhat higher when the inner chamber volume was held constant during axial compression in comparison to the case when the inner chamber pressure was held constant. However, this difference is attributed to the randomness of the in-situ extracted samples. An examination of all of the hollow cylinder test results did not reveal any consistent variation in the  $G'_{z ext}$  values for either the drained or the undrained inner chamber condition. In comparison with the solid cylinders, especially the 60 mm test specimens, the maximum deviator stress  $G'_{z ext}$ , for the hollow cylinders was consistently higher. The differences, however, are considered to be only marginal.

For all clay cylinders, the principal stress ratios expressed as  $(\sigma'_z/\sigma'_r)$  or  $(\sigma'_z/\sigma'_{\theta})$  increased with the increasing axial deformation. A maximum value of the stress ratios was not reached for any of the tests. If the stress ratios in the individual test specimens at the maximum  $\sigma'_z_{ext}$  condition are arbitrarily compared, it is observed that the  $(\sigma'_z/\sigma'_{ro})$  values for the solid cylinder specimens are approximately equal. The solid cylinder  $(\sigma'_z/\sigma'_{ro})$  ratios tend to be higher than the  $(\sigma'_z/\sigma'_r)$  values for the hollow cylinders. However, the hollow cylinder strength as expressed by  $(\sigma'_z/\sigma'_{ro})$  is greater than the solid cylinder strength as expressed by the stress ratio  $(\sigma'_z/\sigma'_{ro})$ .







Fig. 10 Undrained axial compression test. Solid cylinder specimen dia. 60 mm



Fig. 11 Undrained axial compression test. Hollow cylinder specimen with drained inner chamber and  $\sigma_{ro} = \sigma_{ri}$ 

.

.



Fig. 12 Undrained axial compression test. Hollow cylinder specimen with undrained inner chamber

The radial stress  $\sigma_{ri}$  at the inside face of all hollow cylinder specimens which were subjected to axial compression with constant volume of the inner chamber, increased during the initial test stages and later decreased as shown by the variation of the total stress ratio  $\sigma_{ri}/\sigma_{ro}$  in Fig. 12. The initial value of  $\sigma_{ri}/\sigma_{ro}$  corresponds to the stress condition in the test specimen at the end of consolidation. For the hollow cylinder test with a drained inner chamber and constant chamber pressures  $\sigma_{ro} = \sigma_{ri}$ , a volume decrease in the inner chamber occured for all of the tests, as exemplified by the plot of  $(\Delta V/V)_i$  in Fig. 11.

#### 4 SUMMARY

From the presented experimental results, it is shown that during consolidation of the hollow cylinder clay specimen under an all-round pressure, the radial strain  $\mathcal{E}_{r}$  was much larger than the circumferential strain  $\mathcal{E}_{\Theta}$ . The radial effective stress  $\sigma'_{r}$  in the cylinder wall was found to be greater than the circumferential effective stress  $\sigma'_{\Theta}$  during axial compression of the hollow cylinder under undrained condition. The deviator stress  $\sigma'_{z ext}$  at failure for the hollow cylinders was marginally higher than the maximum deviator stress for the solid samples with 35 mm or 60 mm diameter. The deformation characteristics of solid cylinders as expressed by the pore-water pressure changes during axial compression in the undrained state, were dissimilar for the test cylinders with 35 mm and 60 mm diameter in spite of similarity of the test boundary conditions.

#### ACKNOWLEDGEMENTS

The work reported herein was done in 1966-67 when the Author was employed at the Swedish Geotechnical Institute. Part of the Author's funds during this period were provided by a grant from the Swedish National Council for Building Research. To both these institutions, the Author expresses his sincere gratitude.

Acknowledgement is made of the assistance at the design of the test apparatus provided by Mr A. Hallén, Mechanical Department of the Institute.

#### APPENDIX

Formulae for Strain and Stress Computations in Hollow Cylinder Specimen.

Compressive strains and stresses are reckoned positive in the following equations. All stresses are assumed to be effective stresses unless specified otherwise.

<u>Axial Strain</u>  $\mathcal{E}_{z}$  - is computed as the ratio<sup>4</sup> of the change in cylinder height  $\Delta h$  to the initial height h of the specimen, thus

$$\varepsilon_z = \frac{\Delta h}{h}$$
(1)

For the consolidation phase of test, h corresponds to the cylinder height after trimming of the sample, while for the axial compression test h corresponds to the specimen height at the end of consolidation.

Volumetric Strains  $(\Delta V/V)_i$ ,  $(\Delta V/V)_s$  - The volumetric change in the inside chamber  $(\Delta V)_i$  and the clay cylinder  $(\Delta V)_s$  are expressed as the volumetric strains  $(\Delta V/V)_i$  and  $(\Delta V/V)_s$  referenced respectively to the volume of the inside chamber  $V_i$  and the clay cylinder  $V_s$ . For the consolidation test,  $V_i$  and  $V_s$  correspond to the specimen volume after trimming the sample.

The volumetric strain (  $\Delta V/V$  ); in the hollow cylinder during axial compression, corresponds to the volume of inner chamber at the end of consolidation.

Boundary Strains  $\mathcal{E}_{\Theta i} = \mathcal{E}_{ri}$  and  $\mathcal{E}_{\Theta o} = \mathcal{E}_{ro}$  - The boundary strain  $\mathcal{E}_{\Theta i} = \mathcal{E}_{ri}$  at the inner circumferential plane of hollow cylinder is computed from the known volumetric strain ( $\Delta V/V$ )<sub>i</sub> and the compatibility relationship, assuming small strains as

$$\left(\frac{\Delta V}{V}\right)_{i} = \varepsilon_{z} + 2\varepsilon_{\Theta i} = \varepsilon_{z} + 2\varepsilon_{r i}$$
<sup>(2)</sup>

4) See foot-note 2 on page 14

Similarly the outer boundary strain  $\varepsilon_{\Theta_0} = \varepsilon_{ro}$  is computed from

$$\left(\frac{\Delta V}{V}\right)_{o} = \varepsilon_{z} + 2\varepsilon_{\theta o} = \varepsilon_{z} + 2\varepsilon_{ro}$$
(3)

1

where  $\left(\left.\Delta V/V\right.\right)_{o}$  is the volumetric strain for the clay cylinder and the inner chamber, thus

$$\left(\frac{\Delta V}{V}\right)_{o} = \frac{\Delta V_{s} + \Delta V_{i}}{V_{s} + V_{i}}$$
(4)

<u>Radial Strain  $\varepsilon_r$ </u> - is computed from the known boundary strains  $\varepsilon_{\theta i} = \varepsilon_{ri}$ and  $\varepsilon_{\theta o} = \varepsilon_{ro}$  and is expressed as the unit change in the finite cylinder thickness ( $\Gamma_o - \Gamma_i$ ), thus

$$\varepsilon_{r} = \frac{\varepsilon_{\theta o} r_{o} - \varepsilon_{\theta i} r_{i}}{r_{o} - r_{i}}$$
(5)

where  $\Gamma_{\!_{O}}$  and  $\Gamma_{\!_{i}}$  are the outside and inside radii respectively, of the test cylinder.

 $\underbrace{Circumferential Strain \ \epsilon_{\theta}}_{relationship written \ as} - is calculated from the volume compatibility$ 

$$\left(\frac{\Delta V}{V}\right)_{s} = \varepsilon_{z} + \varepsilon_{r} + \varepsilon_{\theta}$$
(6)

where (  $\Delta V/V$  )<sub>s</sub> is the clay cylinder strain and the strains  $\varepsilon_z$  and  $\varepsilon_r$  are computed from Eqs. 1 and 5, respectively.

<u>Axial Stress</u>  $\sigma'_{z}$  - In the absence of an externally applied axial load, the axial stress  $\sigma'_{z \text{ int}}$  due to unequal chamber pressures in the hollow cylinder is calculated from the requirement of equilibrium as,

$$\sigma'_{z \text{ int}} = \frac{\sigma'_{ro} r_{o}^{2} - \sigma'_{ri} r_{i}^{2}}{r_{o}^{2} - r_{i}^{2}}$$
(7)

where  $\sigma'_{ro}$  and  $\sigma'_{ri}$  are the outside and inside chamber pressures, respectively. The externally applied axial load P causes a deviator stress  $\sigma'_{z ext}$  to act upon the test specimen given by

$$\sigma'_{z \text{ ext}} = \frac{P}{A_s}$$
(8)

where A<sub>5</sub> is the current cross-sectional area of the test cylinder. The average axial stress  $\sigma'_z$  is then given by

7

$$\sigma'_{z} = \sigma'_{z ext} + \sigma'_{z int} = \frac{P}{A_{s}} + \frac{\sigma'_{ro} r_{o}^{2} - \sigma'_{ri} r_{i}^{2}}{\sigma_{o}^{2} - r_{i}^{2}}$$
(9)

Radial Stress  $\sigma'_{r}$  - is taken as the mean of the known outer and inner boundary radial stresses as

$$\sigma'_{r} = \frac{\sigma'_{ro} + \sigma'_{ri}}{2}$$
(10)

<u>Circumferential Stress</u>  $\sigma_{\theta}'$  - is computed from the requirement of equilibrium in the lateral direction of the test cylinder and is given by

$$\sigma_{\theta}' = \frac{\sigma_{r_0}' r_0 - \sigma_{r_1}' r_i}{r_0 - r_i}$$
(11)

٤

•

,

,

·

## STATENS GEOTEKNISKA INSTITUT

Swedish Geotechnical Institute

2

4

٤

,

4

2

## SÄRTRYCK OCH PRELIMINÄRA RAPPORTER

Reprints and preliminary reports

	,		
			Pris kr. (Sw. crs.)
No	n.		Out of
1.	. Views on the Stability of Clay Slopes. J. Osterman	1960	print
2.	. Aspects on Some Problems of Geotechnical Chemistry. R. Söderblom	1960	»
З.	Contributions to the Fifth International Conference on Soil Mechanics and Foundation Engineering, Paris 1961. Part I.	1961	*
	<ol> <li>Research on the Texture of Granular Masses.</li> <li><i>T. Kallstenius &amp; W. Bergau</i></li> </ol>		
	<ol> <li>Relationship between Apparent Angle of Friction – with Effective Stresses as Parameters – in Drained and in Consolidated-Undrained Triaxial Tests on Satu- rated Clay. Normally-Consolidated Clay. S. Odenstad</li> <li>Development of two Modern Continuous Sounding Me- thods. T. Kallstenius</li> </ol>		
	<ol> <li>In Situ Determination of Horizontal Ground Movements.</li> <li><i>T. Kallstenius &amp; W. Bergau</i></li> </ol>		
4.	Contributions to the Fifth International Conference on Soil Mechanics and Foundation Engineering, Paris 1961. Part II.	1961	5:—
	Suggested Improvements in the Liquid Limit Test, with Reference to Flow Properties of Remoulded Clays. R. Karlsson		
5.	On Cohesive Soils and Their Flow Properties. R. Karlsson	1963	10:
6.	Erosion Problems from Different Aspects.	1964	10:—
	1. Unorthodox Thoughts about Filter Criteria. W. Kjellman		
	2. Filters as Protection against Erosion. P. A. Hedar		
	<ol> <li>Stability of Armour Layer of Uniform Stones in Running Water. S. Andersson</li> </ol>		
	<ol> <li>Some Laboratory Experiments on the Dispersion and Erosion of Clay Materials. R. Söderblom</li> </ol>		
7.	Settlement Studies of Clay.	1964	10:-
	<ol> <li>Influence of Lateral Movement in Clay Upon Settle- ments in Some Test Areas. J. Osterman &amp; G. Lindskog</li> </ol>		
	<ol> <li>Consolidation Tests on Clay Subjected to Freezing and Thawing. J. G. Stuart</li> </ol>		
8.	Studies on the Properties and Formation of Quick Clays. J. Osterman	1965	5:—
9.	Beräkning av pålar vid olika belastningsförhållanden. B. Broms	1965	30: —
	1. Beräkningsmetoder för sidobelastade pålar.		
	2. Brottlast för snett belastade pålar.		
	3. Beräkning av vertikala pålars bärförmåga.		
10.	Triaxial Tests on Thin-Walled Tubular Samples.	1965	5:
	<ol> <li>Effects of Rotation of the Principal Stress Axes and of the Intermediate Principal Stress on the Shear Strength. B. Broms &amp; A. O. Casbarian</li> </ol>		
	<ol> <li>Analysis of the Triaxial Test-Cohesionless Soils.</li> <li>B. Broms &amp; A. K. Jamal</li> </ol>		
11.	Något om svensk geoteknisk forskning. B. Broms	1966	5 <b>: —</b>
12.	Bärförmåga hos pålar slagna mot släntberg. B. Broms	1966	15:—
13.	Förankring av ledningar i jord. B. Broms & O. Orrje	1966	5:-
14.	Ultrasonic Dispersion of Clay Suspensions. R. Pusch	1966	5:—
15.	Investigation of Clay Microstructure by Using Ultra-Thin Sections. R. Pusch	1966	10:
16.	Stability of Clay at Vertical Openings. B. Broms & H. Bennermark	1967	10: —

.

No			Pris kr. (Sw. crs.)
17. Om påls	slagning och pålbärighet.	1967	5:
1. Dr	agsprickor i armerade betongpålar. S. Sahlin		
2. Sp rac	rickbildning och utmattning vid slagning av arme- de modellpålar av betong. B-G. Hellers		
3. Bä sp	righet hos släntberg vid statisk belastning av berg- ets. Resultat av modellförsök. S-E. Rehnman		
4. Ne	gativ mantelfriktion. B. H. Fellenius		
5. Gr sö	undläggning på korta pålar. Redogörelse för en för- ksserie på NABO-pålar. <i>G. Fjelkner</i>		
6. Kr	okiga pålars bärförmåga. <i>B. Broms</i>		
18. Pålgrup	pers bärförmåga. B. Broms	1967	10:
19. Om stor	opslagning av stödpålar. <i>L. Hellman</i>	1967	5:—
20. Contribu Society	itions to the First Congress of the International of Rock Mechanics, Lisbon 1966.	1967	5: —
1. A	Note on Strength Properties of Rock. B. Broms		
2. Te	nsile Strength of Rock Materials. B. Broms		
21. Recent	Quick-Clay Studies.	1967	10:—
1. Re	cent Quick-Clay Studies, an Introduction. R. Pusch		
2. Ch <i>R.</i>	emical Aspects of Quick-Clay Formation. Söderblom		
3. Qi	ick-Clay Microstructure. R. Pusch		
22. Jordtryc	k vid friktionsmaterial.	1967	30:
1. Re <i>B.</i>	sultat från mätning av jordtryck mot brolandfäste. Broms & I. Ingelson		
2. Jo	rdtryck mot oeftergivliga konstruktioner. B. Broms		
3. Me oc pla	etod för beräkning av sambandet mellan jordtryck h deformation hos främst stödmurar och förankrings- attor i friktionsmaterial. <i>B. Broms</i>		
4. Ве	räkning av stolpfundament. B. Broms		
23. Contribu Strength	utions to the Geotechnical Conference on Shear Properties of Natural Soils and Rocks, Oslo 1967.	1968	10: —
1. Ef Cl	fective Angle of Friction for a Normally Consolidated ay. <i>R. Brink</i>		
2. Sh ter Co	ear Strength Parameters and Microstructure Charac- istics of a Quick Clay of Extremely High Water ontent. R. Karlsson & R. Pusch		
3. Ra Inc <i>R.</i>	tio c/p' in Relation to Liquid Limit and Plasticity dex, with Special Reference to Swedish Clays. Karlsson & L. Viberg		
24. A Tech Pusch	nique for Investigation of Clay Microstructure. R.	1968	22:
25. A New S Resistar	Settlement Gauge, Pile Driving Effects and Pile nce Measurements.	1968	10:
1. Ne <i>U</i> .	ew Method of Measuring in-situ Settlements. Bergdahl & B. Broms		
2. Efi <i>O</i> .	iects of Pile Driving on Soil Properties. Orrje & B. Broms		
3. En <i>B</i> .	d Bearing and Skin Friction Resistance of Piles. Broms & L. Hellman		
26. Sättning	ar vid vägbyggnad.	1968	20:
Föredra I Voksei	g vid Nordiska Vägtekniska Förbundets konferens nåsen, Oslo 25–26 mars 1968.		
1. Ge nir	eotekniska undersökningar vid bedömning av sätt- ngar. <i>B. Broms</i>		
2. Te för	knisk-ekonomisk oversikt over anläggningsmetoder reducering av sättningar i vägar. A. Ekström		
3. Sä på	ttning av verkstadsbyggnad i Stenungsund uppförd normalkonsoliderad lera. B. Broms & O. Orrje	1000	164
27. Bartorm bergspe	aga nos siantberg við statisk belastning av ts. Resultat från modellförsök. S-E. Rehnman	1900	10:-

ъ

No.		Pris kr. (Sw. crs.)
28. Bidrag till Nordiska Geoteknikermötet i Göteborg den 5-7 september 1968	1968	15:-
<ol> <li>Nordiskt geotekniskt samarbete och nordiska geotek- nikermöten. N. Flodin</li> </ol>		
2. Några resultat av belastningsförsök på lerterräng speciellt med avseende på sekundär konsolidering. G. Lindskog		
<ol> <li>Sättningar vid grundläggning med plattor på morän- lera i Lund. S. Hansbo, H. Bennermark &amp; U. Kihlblom</li> </ol>		
4. Stabilitetsförbättrande spontkonstruktion för bankfyll- ningar. O. Wager		
5. Grundvattenproblem i Stockholms city. G. Lindskog & U. Bergdahi		
b. Aktuell svensk geoteknisk forskning. B. Broms 29. Classification of Soils with Reference to Compaction.	1968	5:
B, Broms & L. Forssblad		
<ol> <li>Flygbildstolkning som hjälpmedel vid översiktliga grundundersökningar.</li> </ol>	1969	10:
<ol> <li>Flygbildstolkning för jordartsbestämning vid samhälls- planering 1-2. U. Kihlblom, L. Viberg &amp; A. Heiner</li> </ol>		
<ol> <li>Identifiering av berg och bedömning av jorddjup med hjälp av flygbilder. U. Kihlblom</li> </ol>		
31. Nordiskt sonderingsmöte i Stockholm den 5-6 oktober 1967. Föredrag och diskussioner.	1969	30:
<ol> <li>Contributions to the 3rd Budapest Conference on Soil Mechanics and Foundation Engineering, Budapest 1968.</li> </ol>	1969	10:-
<ol> <li>Swedish Tie-Back Systems for Sheet Pile Walls. B. Broms</li> </ol>		
<ol> <li>Stability of Cohesive Soils behind Vertical Openings in Sheet Pile Walls. Analysis of a Recent Failure.</li> <li>Broms &amp; H. Bennermark</li> </ol>		
33. Seismikdag 1969. Symposium anordnat av Svenska Geotek- niska Föreningen den 22 april 1969.	1970	20: —
34. Något om geotekniken i Sverige samt dess roll i plane- rings- och byggprocessen. Några debattinlägg och allmänna artiklar.	1970	15: —
1. Geoteknikern i det specialiserade samhället.		
<ul> <li>B. Broms</li> <li>2. Diskussionsinlägg vid konferens om geovetenskaperna, 7 mars 1969.</li> </ul>		
<ol> <li>Geoteknik i Sverige – utveckling och utvecklingsten- denser.</li> </ol>		
<ol> <li>Geotekniska undersökningar och grundläggningsmeto- der.</li> </ol>		
5. Grundläggning på plattor – en allmän översikt.		
<ol> <li>Piles – a New Force Gauge, and Bearing Capacity Calcu- lations.</li> </ol>	1970	10:
1. New Pile Force Gauge for Accurate Measurements of Pile Behavior during and Following Driving. B. Fellenius & Th. Hangen		
<ol> <li>Definition of Annual Activity of Calculating the Ultimate Bearing Capa- city of Piles. A Summary.</li> <li>B. Broms</li> </ol>		
36. Pålslagning. Materialegenskaper hos berg och betong.	1970	10: —
1. Bergets bärförmåga vid punktbelastning. SE. Rehnman		
<ol> <li>Deformationsegenskaper hos slagna betongpålar.</li> <li>B. Fellenius &amp; T. Eriksson</li> </ol>		
37. Jordtryck mot grundmurar.	1970	10: —
1. Jordtryck mot grundmurar av Lecablock. SE. Rehnman & B. Broms		
<ol> <li>Beräkning av jordtryck mot källarväggar.</li> <li>B. Broms</li> </ol>		
<ol> <li>Provtagningsdag 1969. Symposium anordnat av Svenska Geotekniska Föreningen den 28 oktober 1969.</li> </ol>	1970	25:

No			Pris kr. (Sw. crs.)
39.	Morändag 1969. Symposium anordnat av Svenska Geotekniska Föreningen den 3 december 1969.	1970	25:—
40.	<ul> <li>Stability and Strengthening of Rock Tunnels in Scandinavia.</li> <li>1. Correlation of Seismic Refraction Velocities and Rock Support Requirements in Swedish Tunnels. O. S. Cecil</li> <li>2. Problems with Swelling Clays in Norwegian Under- ground Constructions in Hard-Rocks. R. Selmer-Olsen</li> </ul>	1971	25: —
41.	Stålpålars bärförmåga. Resultat av fältförsök med lätta slagdon. G. Fjelkner	1971	30:
42.	Contributions to the Seventh International Conference on Soil Mechanics and Foundation Engineering, Mexico 1969.	1971	15: —
43.	Centrically Loaded Infinite Strip on a Single-Layer Elastic Foundation – Solution in Closed Form According to the Boussinesq Theory. B-G. Hellers & O. Orrje	1972	20:
44.	<ul> <li>On the Bearing Capacity of Driven Piles.</li> <li>1. Methods Used in Sweden to Evaluate the Bearing Capacity of End-Bearing Precast Concrete Piles. B. Broms &amp; L. Hellman</li> <li>2. Discussions at the Conference, Behaviour of Piles, London 1970. B. Fellenius, B. Broms &amp; G. Fjelkner</li> <li>3. Bearing Capacity of Piles Driven into Rock. With Discussion. S-E. Rehnman &amp; B. Broms</li> <li>4. Bearing Capacity of Cyclically Loaded Piles. B. Broms</li> <li>5. Bearing Capacity of End-Bearing Piles Driven to Rock. S-E. Rehnman &amp; B. Broms</li> </ul>	1972	20: —
45.	<ul> <li>Quality in Soil Sampling.</li> <li>1. Secondary Mechanical Disturbance. Effects in Cohesive Soil Samples. <i>T. Kallstenius</i></li> <li>2. Sampling of Sand and Moraine with the Swedish Foil Sampler. <i>B. Broms &amp; A. Hallén</i></li> </ul>	1972	10: —
46.	Geoteknisk flygbildstolkning. En undersökning av metodens tillförlitlighet. L. Viberg	1972	۳)
47.	Some Experiments on Hollow Cylinder Clay Specimens. A. K. Jamal	1972	10: —

See.